

Vektoridentitäten

$$\begin{array}{ll} \psi = \psi(\vec{r}) & \phi = \phi(\vec{r}) \\ \vec{A} = \vec{A}(\vec{r}) & \vec{B} = \vec{B}(\vec{r}) \end{array}$$

$$\vec{\nabla}(\psi\varphi) = \psi\vec{\nabla}\varphi + \varphi\vec{\nabla}\psi$$

$$\vec{\nabla} \cdot (\varphi \vec{A}) = \varphi \vec{\nabla} \cdot \vec{A} + \vec{A} \cdot \vec{\nabla} \varphi$$

$$\vec{\nabla} \times (\varphi \vec{A}) = \varphi \vec{\nabla} \times \vec{A} - \vec{A} \times \vec{\nabla} \varphi$$

$$\vec{\nabla}(\vec{A} \cdot \vec{B}) = (\vec{A} \cdot \vec{\nabla})\vec{B} + (\vec{B} \cdot \vec{\nabla})\vec{A} + \vec{A} \times (\vec{\nabla} \times \vec{B}) + \vec{B} \times (\vec{\nabla} \times \vec{A})$$

$$\vec{\nabla} \cdot (\vec{A} \times \vec{B}) = \vec{B} \cdot (\vec{\nabla} \times \vec{A}) - \vec{A} \cdot (\vec{\nabla} \times \vec{B})$$

$$\vec{\nabla} \times (\vec{A} \times \vec{B}) = (\vec{B} \cdot \vec{\nabla})\vec{A} - \vec{B}(\vec{\nabla} \cdot \vec{A}) + \vec{A}(\vec{\nabla} \cdot \vec{B}) - (\vec{A} \cdot \vec{\nabla})\vec{B}$$

$$\vec{\nabla} \cdot (\vec{\nabla} \varphi) = \operatorname{div}(\operatorname{grad} \varphi) = \Delta \varphi$$

$$\vec{\nabla} \cdot (\vec{\nabla} \times \vec{A}) = \operatorname{div}(\operatorname{rot} \vec{A}) = 0$$

$$\vec{\nabla} \times (\vec{\nabla} \varphi) = \operatorname{rot}(\operatorname{grad} \varphi) = 0$$

$$\vec{\nabla} \times (\vec{\nabla} \times \vec{A}) = \operatorname{rot}(\operatorname{rot} \vec{A}) = \operatorname{grad}(\operatorname{div} \vec{A}) - \Delta \vec{A}$$