

# 3rd Austrian Hungarian Workshop on Trojans and related Topics

## Stability of P-Type Orbits in Exoplanetary systems

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# Stability of P-Type Orbits in Exoplanetary systems

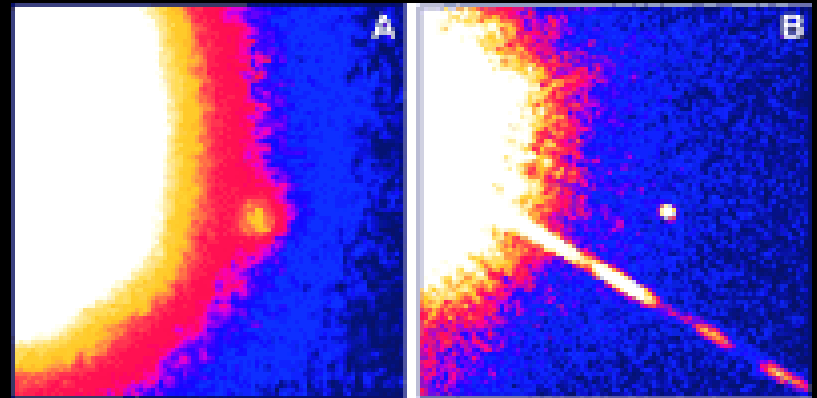
- Planets around binaries
- The calculations of planetary orbits
  - Modell
  - Initial conditions
- The results
  - Dependence from the eccentricity
  - Dependence from the inclination

# Planets around binaries

- Possible planetary orbits in binaries
- Are there any planets found in binary systems

# Planets around binaries

- Possible planetary orbits in binaries
- Are there any planets found in binary systems



# The calculations of planetary orbits: Modell

- Description of calculation
- Integration of the orbit

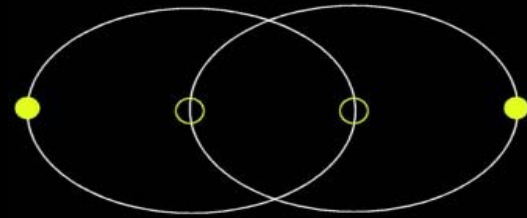
# Description of calculation

- The restricted three body problem
  - Two stars  $m_1$ ,  $m_2$  and a third body  $m_3=0$
- The stars:
  - Mass ratio:  $m_1=m_2$   $\mu=0.5$
  - Distance between the stars is one
- The planets:
  - Move in the gravitational field of the primaries
  - Follow the equations of motion of the restricted three body problem

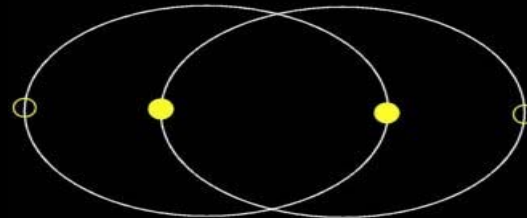
# Initial Conditions: The stars

- Different eccentricities
  - $e = 0 - 0.5$
  - Step = 0.05
- Two initial positions:
  - Apoapsis
  - Periapsis

Apoapsis

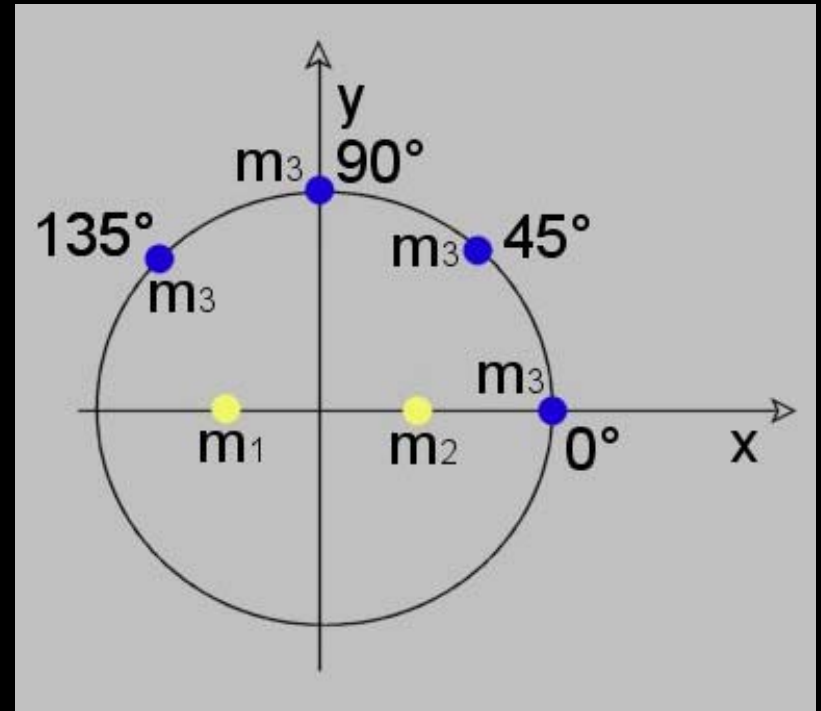


Periapsis



# Initial Conditions: The planets

- The planets start on circular orbits
- Different inclinations  
 $0^\circ < i < 50^\circ$   
Step:  $2.5^\circ$
- **4 initial positions**
- Different distances from the barycentre





# Integration of the orbit

- Each orbit was integrated until:
  - the planet escaped
  - the integration time limit (50000 periods of the primaries) was reached

# The results

Some examples:

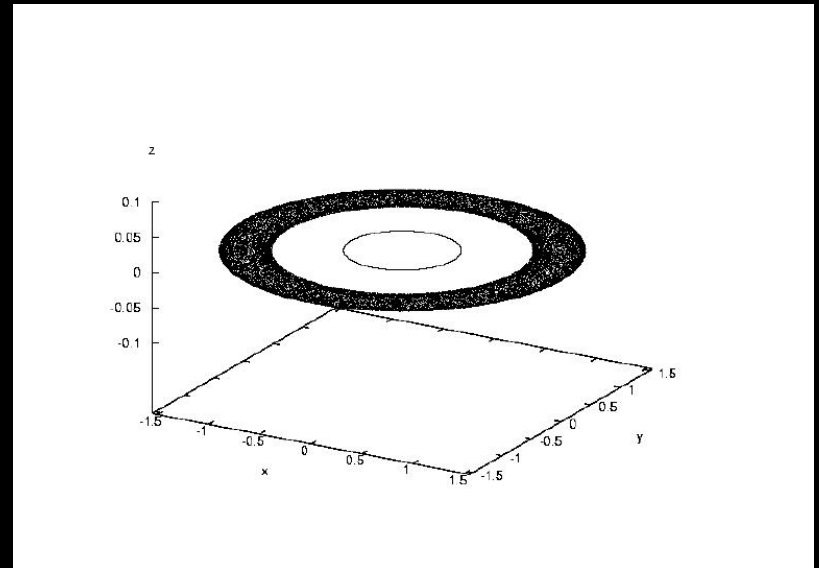
– Planetary orbits with inclination:

»  $i = 0^\circ$

»  $i = 10^\circ$

»  $i = 30^\circ$

»  $i = 50^\circ$



# The results

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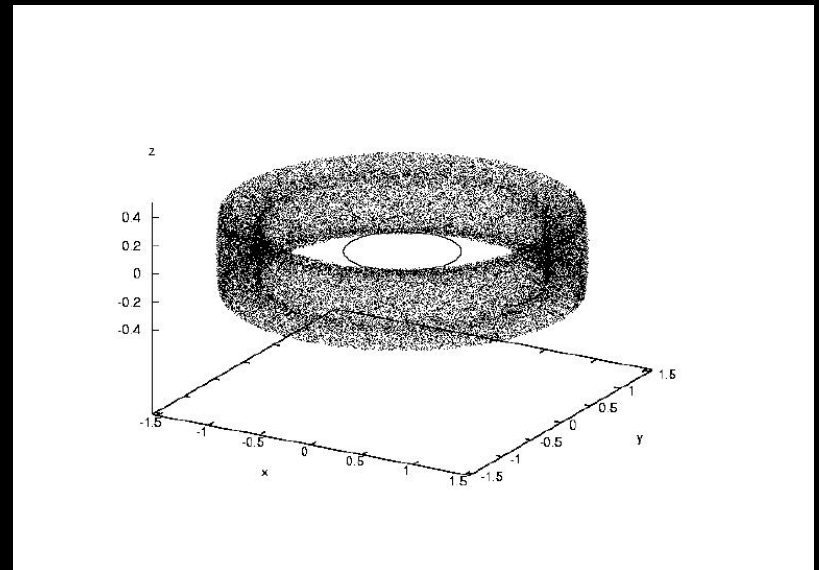
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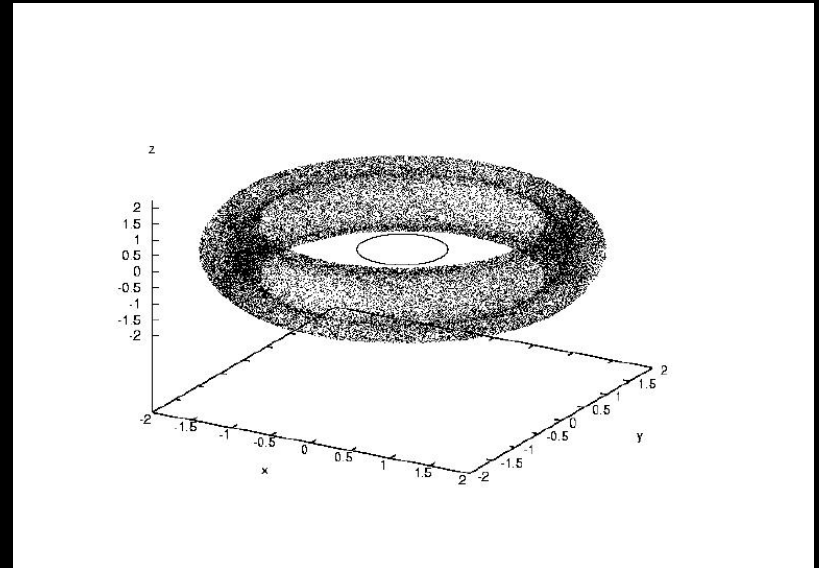
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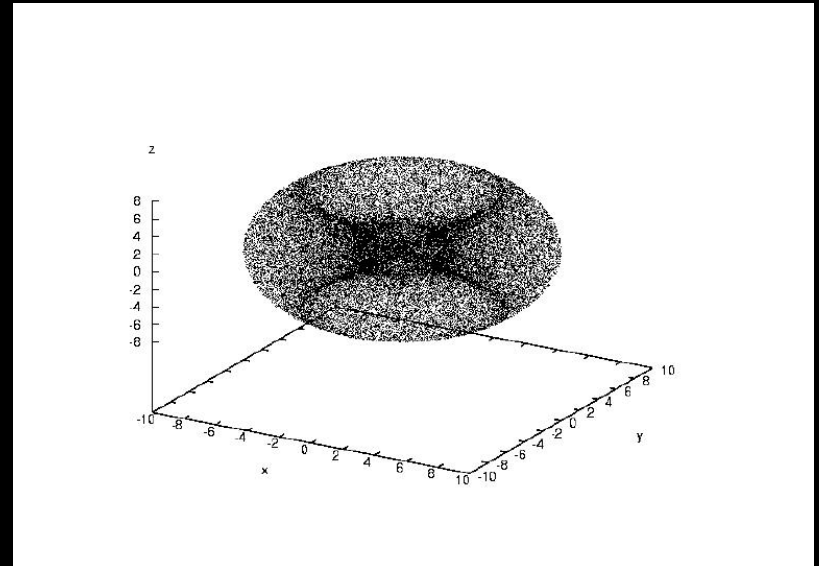
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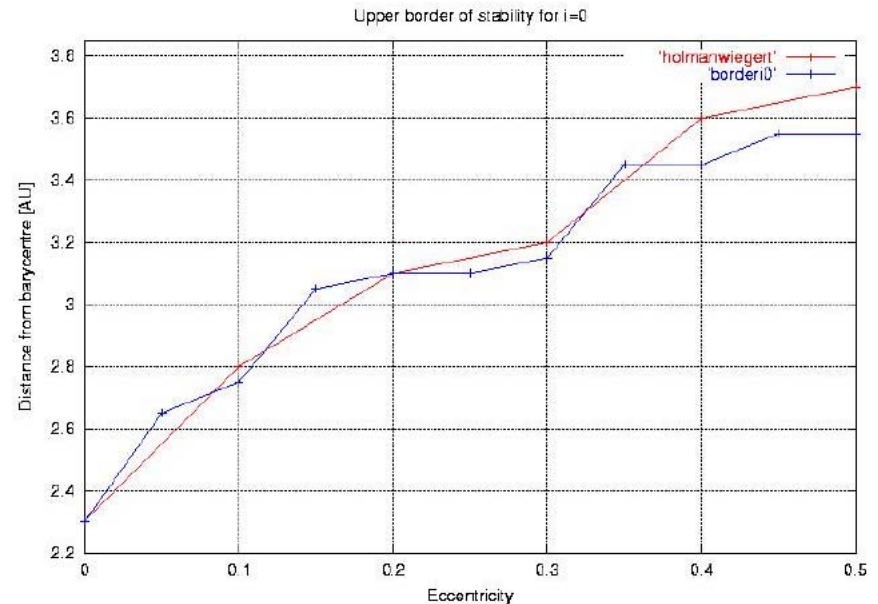


# The results

- **Border of stability**
  - **Absolut upper border**
    - Over this border all orbits were stable
  - **Absolut lower border**
    - Under this border all orbits were unstable
  - **Between those borders: chaotic region**
- **Dependence from the eccentricity**
- **Dependence from the inclination**

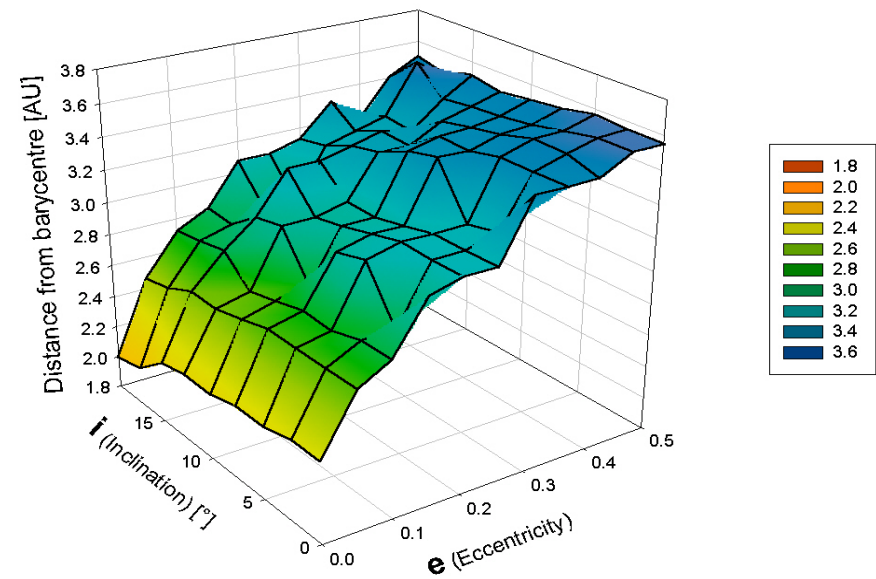
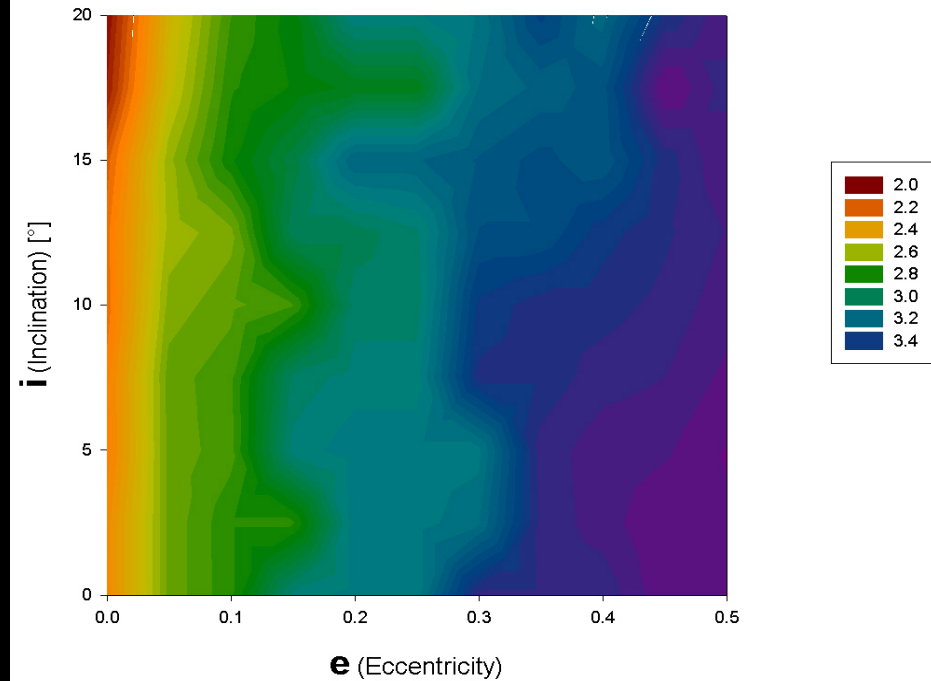
# Dependence from the eccentricity

- Comparison of the border of stability for  $i=0$  with Holman-Wiegert
- The border of stability for different eccentricities and inclinations



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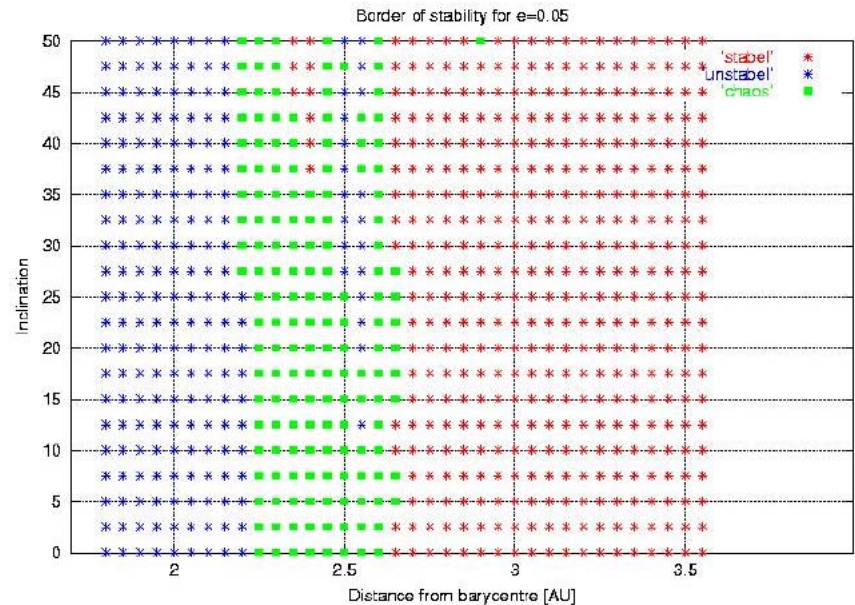
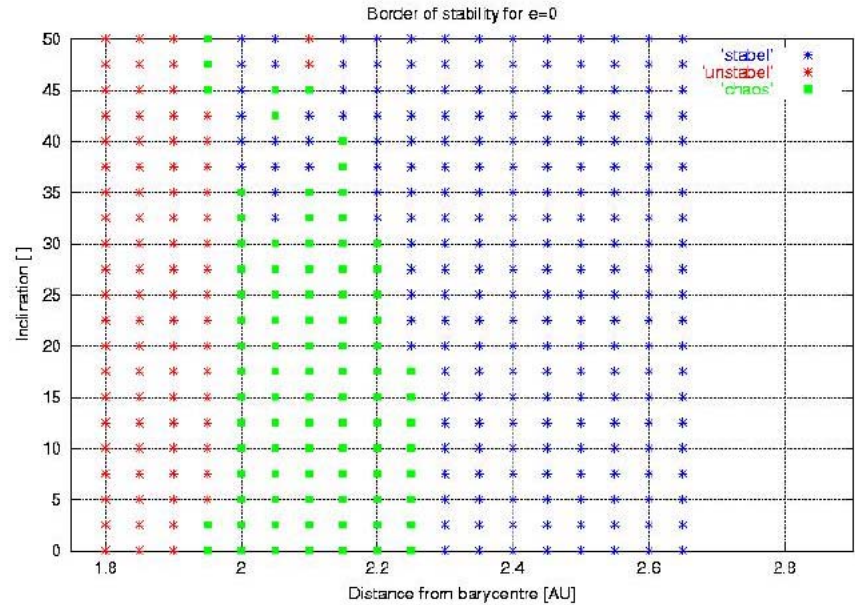
## upper Border





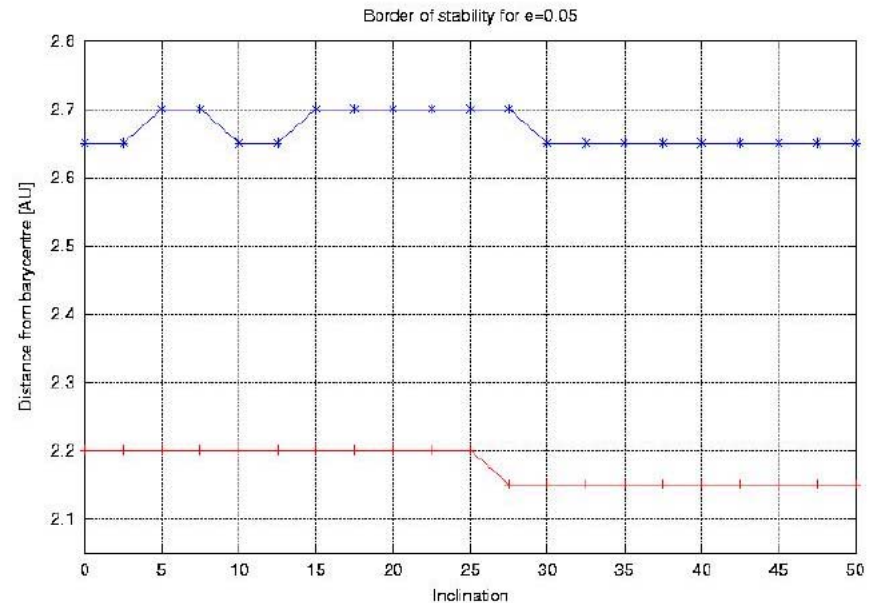
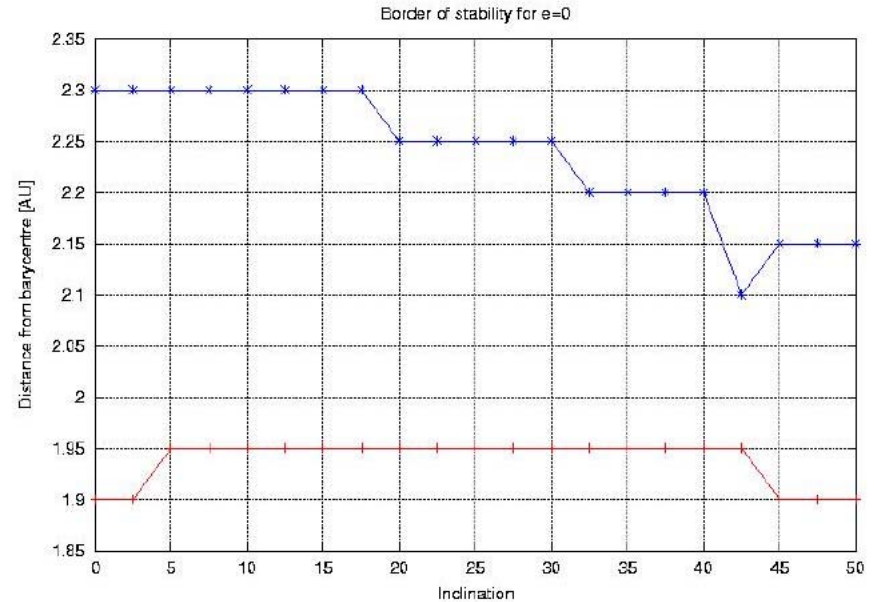
# Dependence from the inclination

- For  $e=0$  and  $0.05$ 
  - Stabel, unstabel and chaotic region
  - Upper und lower border of stability
  - Escape times:
    - For  $e=0$
    - For  $e=0.05$



# Dependence from the inclination

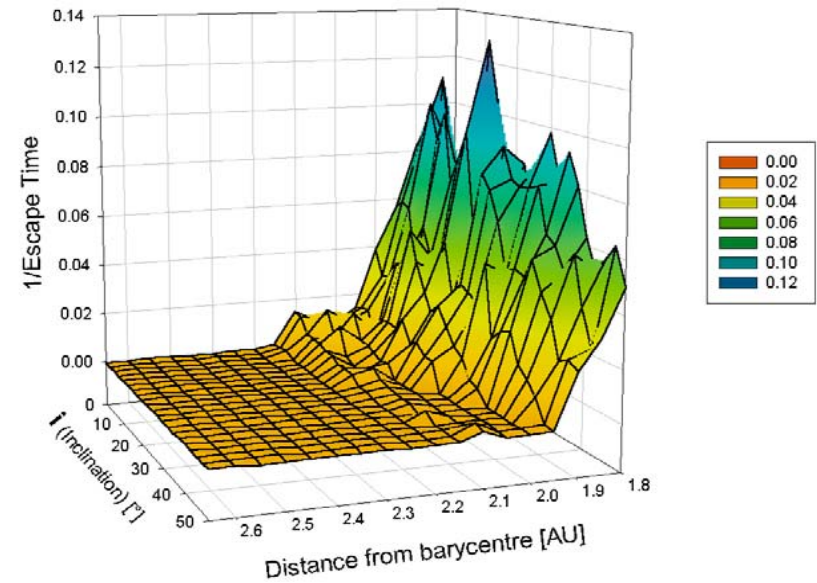
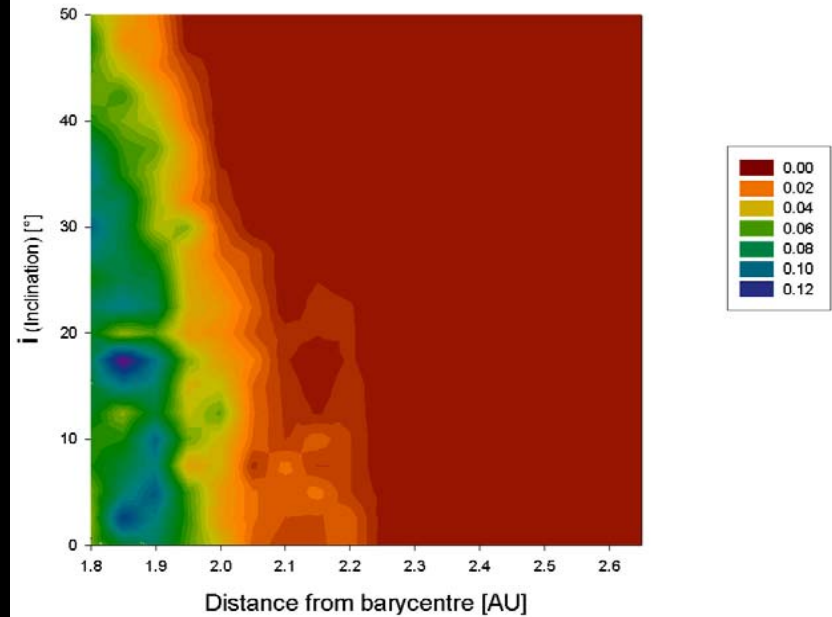
- For  $e=0$  and  $e=0.05$ 
  - Stable, unstable and chaotic region
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    - For  $e=0$
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- For  $e=0$

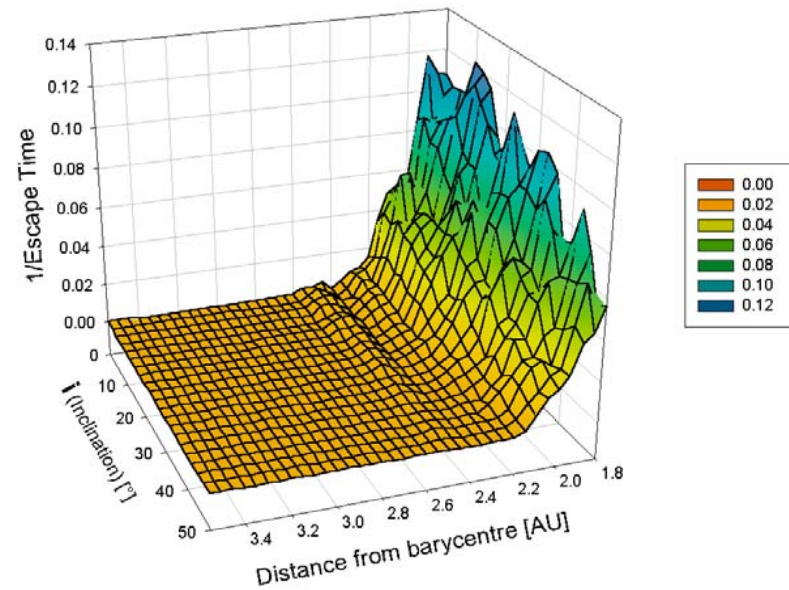
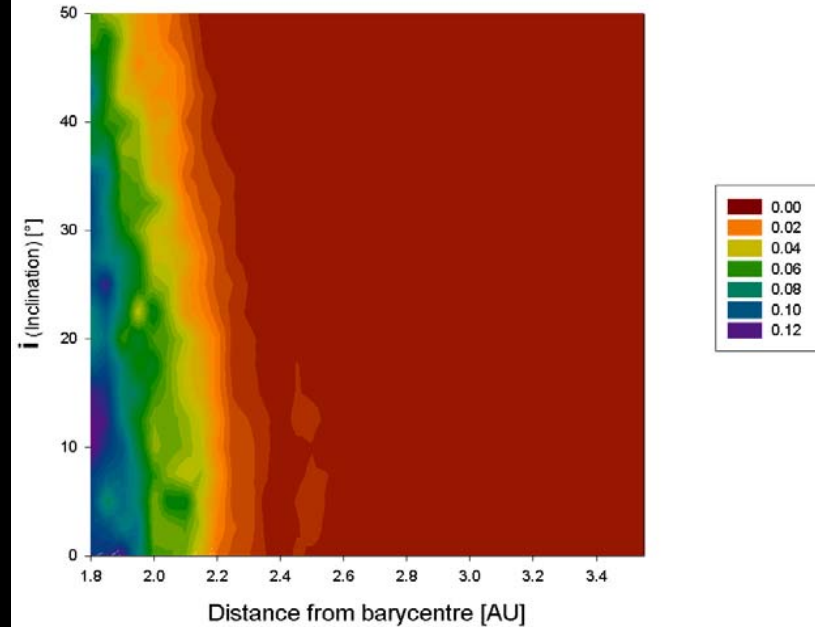
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escape time for  $e=0$



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escape time for  $e=0.05$



# Conclusions

- Lower and upper border decrease slightly with the inclination
- Increase from the border of stability with  $e$  independent from the inclination
- Calculations for more values of the eccentricity and the inclination will be done