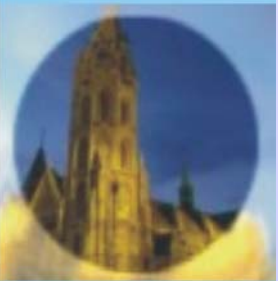


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Hungarian

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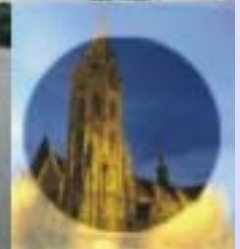


# Some Aspects of NEA Classification



**3. Austrian - Hungarian  
Workshop**

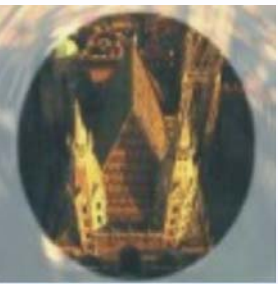
**on Trojans  
and related Topics**



# Why do we need to classify NEAs ?

- NEAs evolve on chaotic orbit
- therefore results for one individual object are „useless“
- one has to derive statistical values
- thus induces some sort of grouping

2 examples shall illustrate the problem →



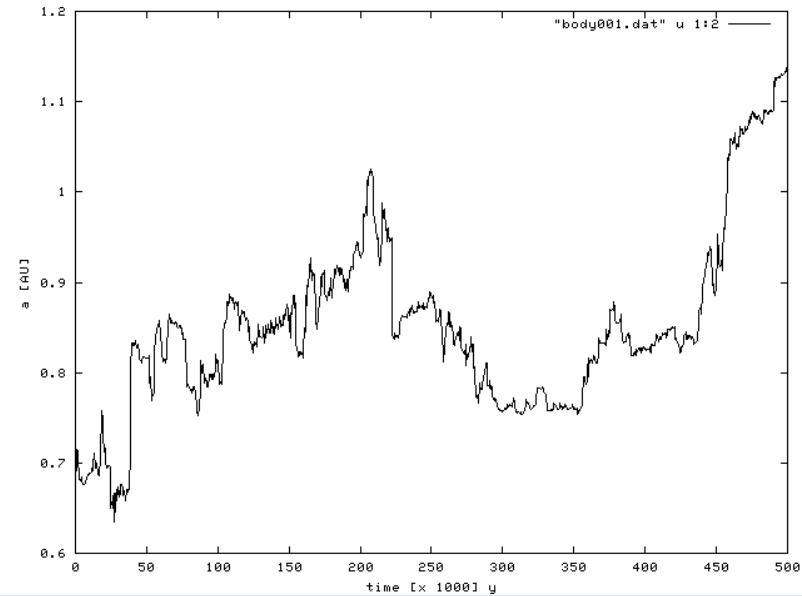
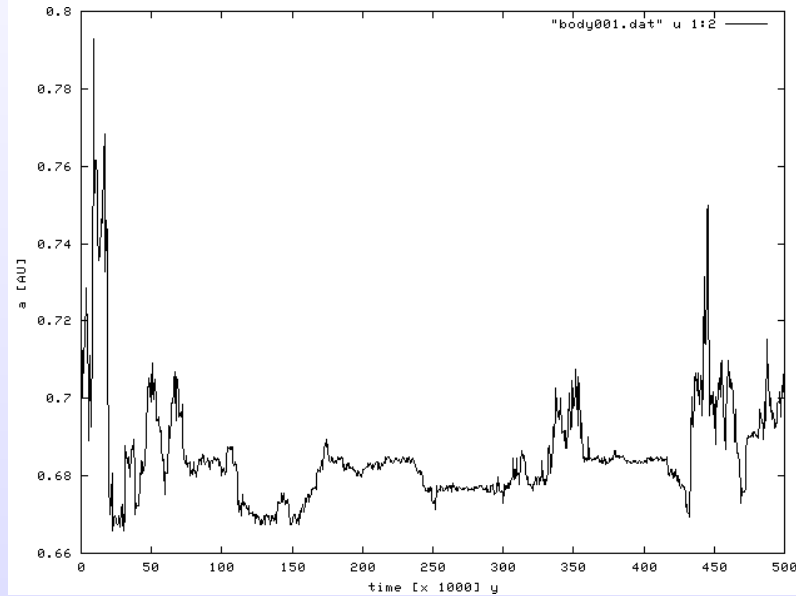
# Example 1

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## Body 001 A

- $a=0.7$  AU,  $e=0.1$ ,  $i=1^\circ$
- $CP_{\text{EARTH}}=5,78E-08$
- $BCN=0$

Pentium II Processor

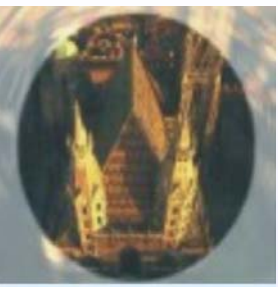
different Integratorstepsize

## Body 001 B

- $a=0.7$  AU,  $e=0.1$ ,  $i=1^\circ$
- $CP_{\text{EARTH}}=6,98E-08$
- $BCN=38$

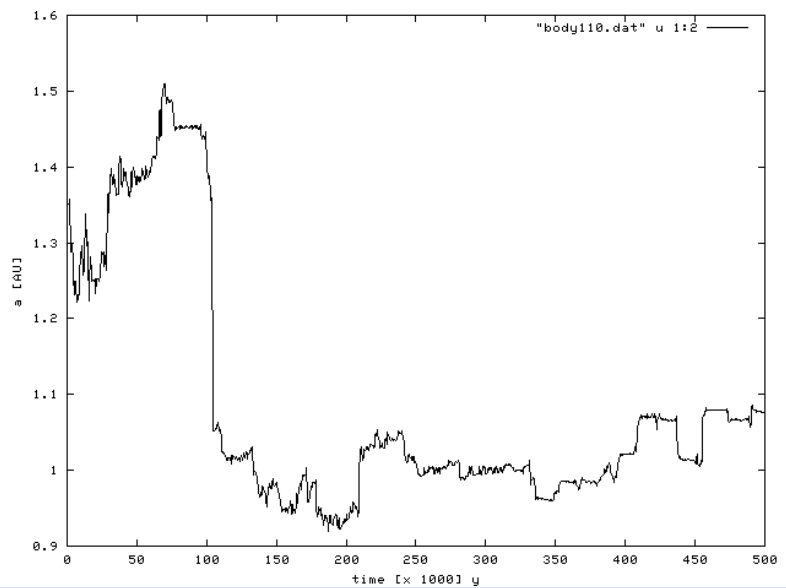
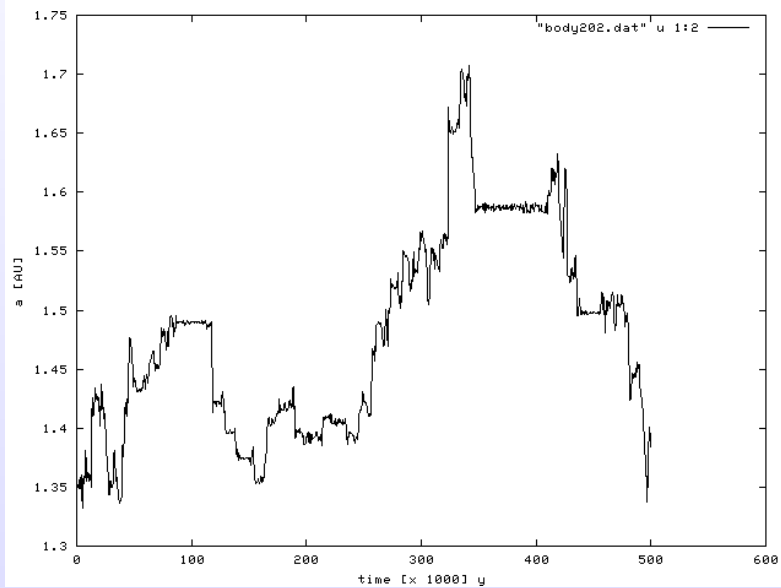
AMD 1800 Processor





# Example 2

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## Body 002 A

- $a=1.35$  AU,  $e=0.4$ ,  $i=1^\circ$
- $CP_{EARTH}=4,21E-08$
- $BCN= 0$

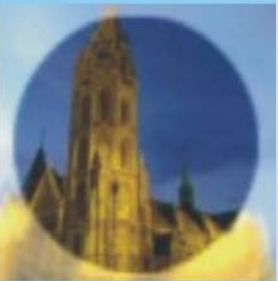
Pentium II Processor

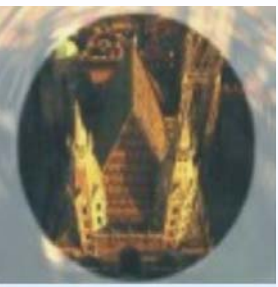
different Integratorstepsize

## Body 002 B

- $a=1.35$  AU,  $e=0.4$ ,  $i=1^\circ$
- $CP_{EARTH}=6,43E-08$
- $BCN= 58$

AMD 1800 Processor



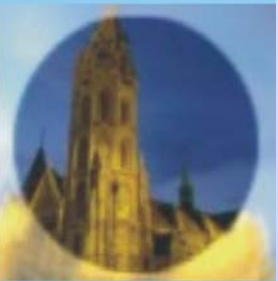


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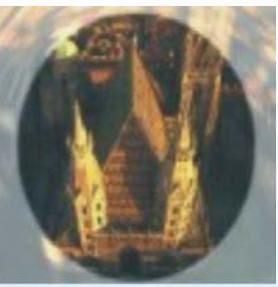
# Grouped Asteroids

## Model 1 (Pentium II)

- Aten (264 bodies) :  $CP_{\text{EARTH}} = 7,85E-08$
- Apollo (348 bodies) :  $CP_{\text{EARTH}} = 5,26E-08$
- Amor (54 bodies) :  $CP_{\text{EARTH}} = 3,79E-09$

## Model 2 (AMD 1800)

- Aten (88 bodies) :  $CP_{\text{EARTH}} = 7,52E-08$
- Apollo (116 bodies) :  $CP_{\text{EARTH}} = 5,20E-08$
- Amor (18 bodies) :  $CP_{\text{EARTH}} = 1,48E-09$

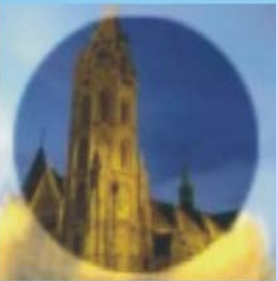


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## First „Rule“

If one deals with NEAs, one has to define groups.

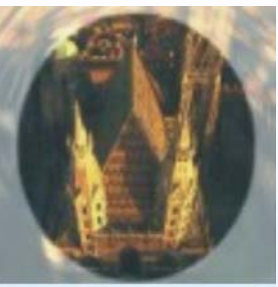
The number of group members must be sufficient large !

## First Problem

The number of group members is NOT constant !

NEAs suffer under MIXING !





# Mixing

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**Dvorak and Freistetter (2001) :**

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720 fictitious asteroids :

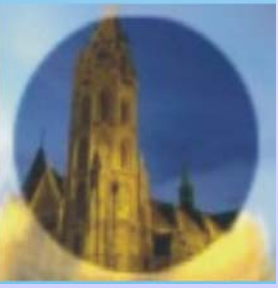
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M e a n P e r c e n t a g e o f M e m b e r s h i p			
S u b a t e n	A t e n	A p o l l o	A m o r
53,74%	70,99%	83,00%	90,43%

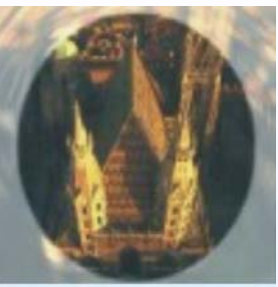
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**Milani et al (1989) :**

89 real asteroids :



M e a n P e r c e n t a g e o f M e m b e r s h i p						
G e o g r a p h o s	T o r o	K o z a i	A l i n d a	E r o s	O l j a t o	C o m e t
75,86%	22,90%	91,70%	55,05%	83,72%	65,13%	84,14%



# Problems due to mixing

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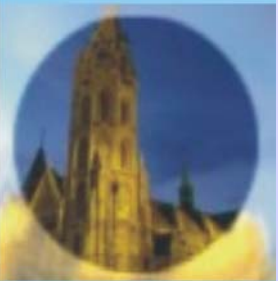
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Example : The APOLLO Group has a mean collision-probability with Earth of ~53 collisions in  $10^9$  years.

BUT : A „mean Apollo“ spends 11% of its time as an Aten, 83 % as an Apollo and 3% as an Amor !

(Dvorak and Freistetter, 2001)

Therefore : The grouping used for calculating statistical properties has to „sufficiently stable“ during integration time.





# New ways of classification

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- „Normal“ classifications are not stable enough.
- A new attempt to classify NEAs is based on the existing classes → „Meta Classification“
- Groups are also based on the dynamical properties → should be more stable than existing ones.



# Border Crossing Numbers

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Border Crossing Number (BCN) :=  
Number of group changes in the  
Aten/Apollo/Amor Classification

Distribution of BCNs was  
checked for 720 asteroids



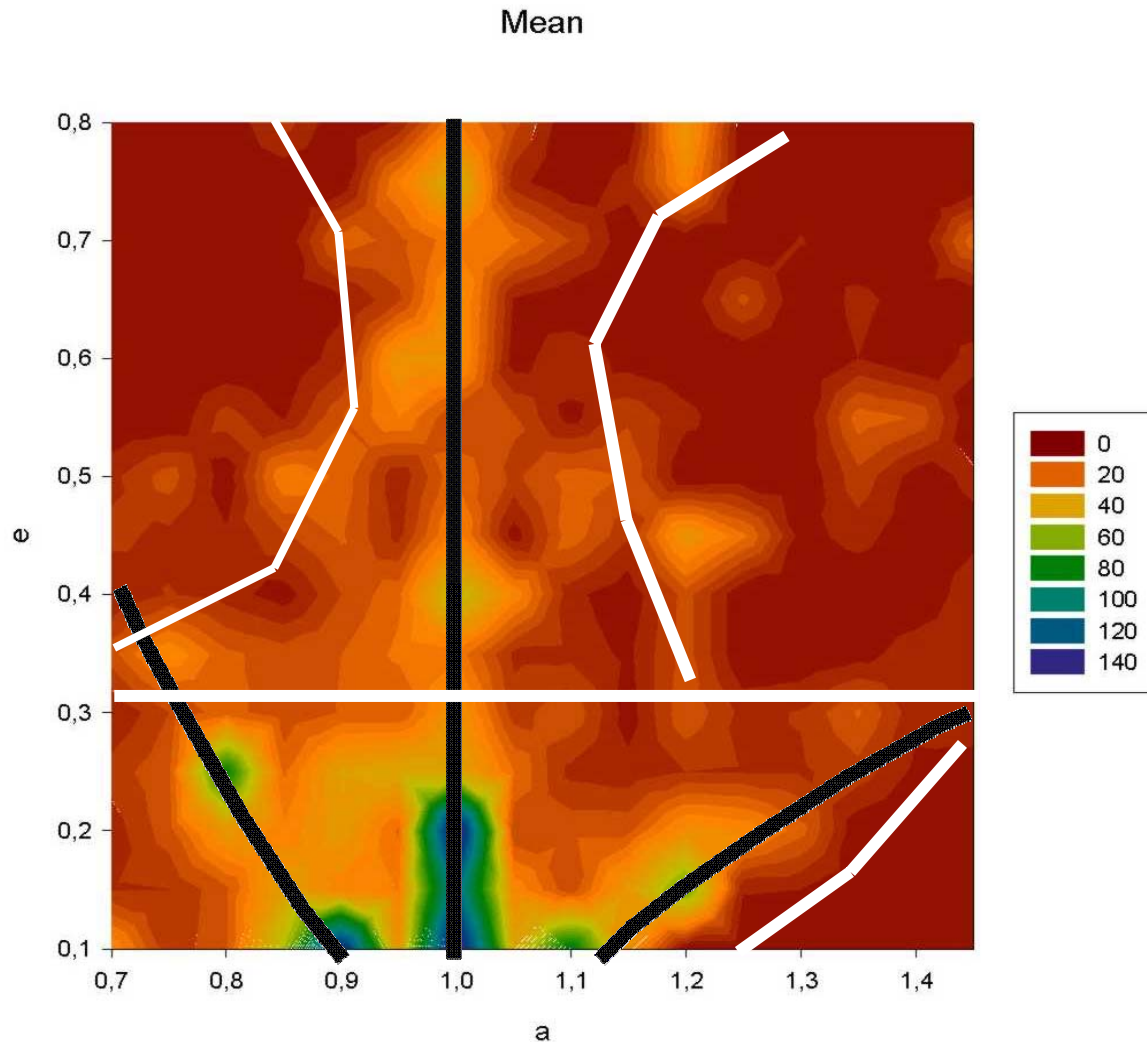
# Border Crossing Numbers

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# Fuzzy Classification

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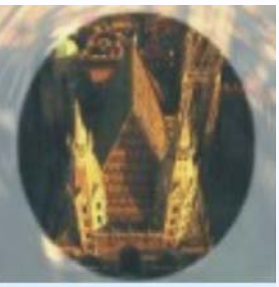
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BCNs investigate the general properties of mixing. For a useful grouping some more details are needed :

- Direction of asteroidal flow in a-e plane
- Speed of asteroidal flow in a-e plane

This information leads to a „fuzzy classification“



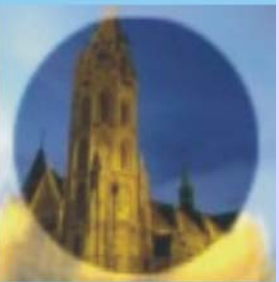


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# Fuzzy Classification

A fuzzy group needs a membership function that gives the grade of membership.

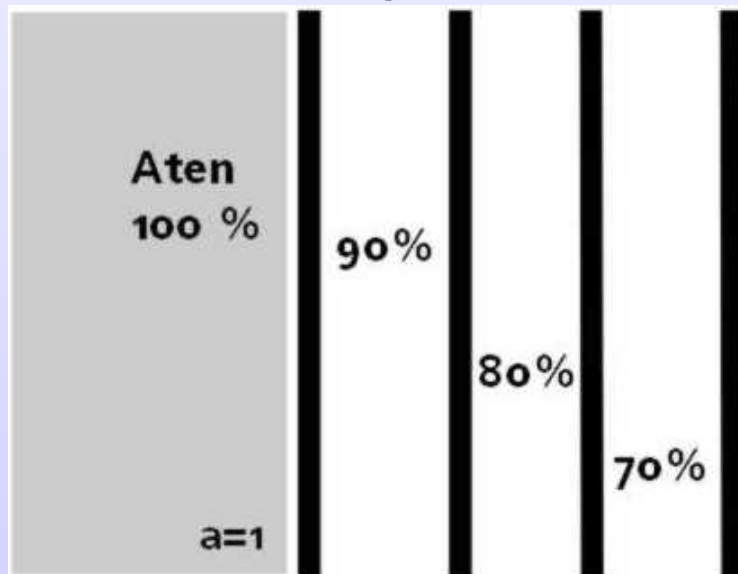
We want to establish a grouping, that gives, for a certain region in a-e space, that mean grade of membership to the classical Aten/Apollo/Amor classification.

This is done by calculation a „vector field“ →

# Fuzzy Classification

How to construct a membership function for NEAs:

1) make copies of the classical border and place them outside the original one :



Because the choice of this borders was „intuitive“ they have to be adjusted.

This is done by calculating the flow around the borders.

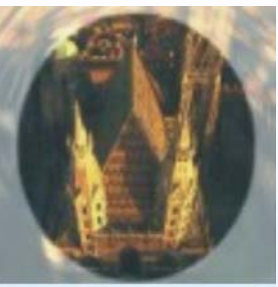
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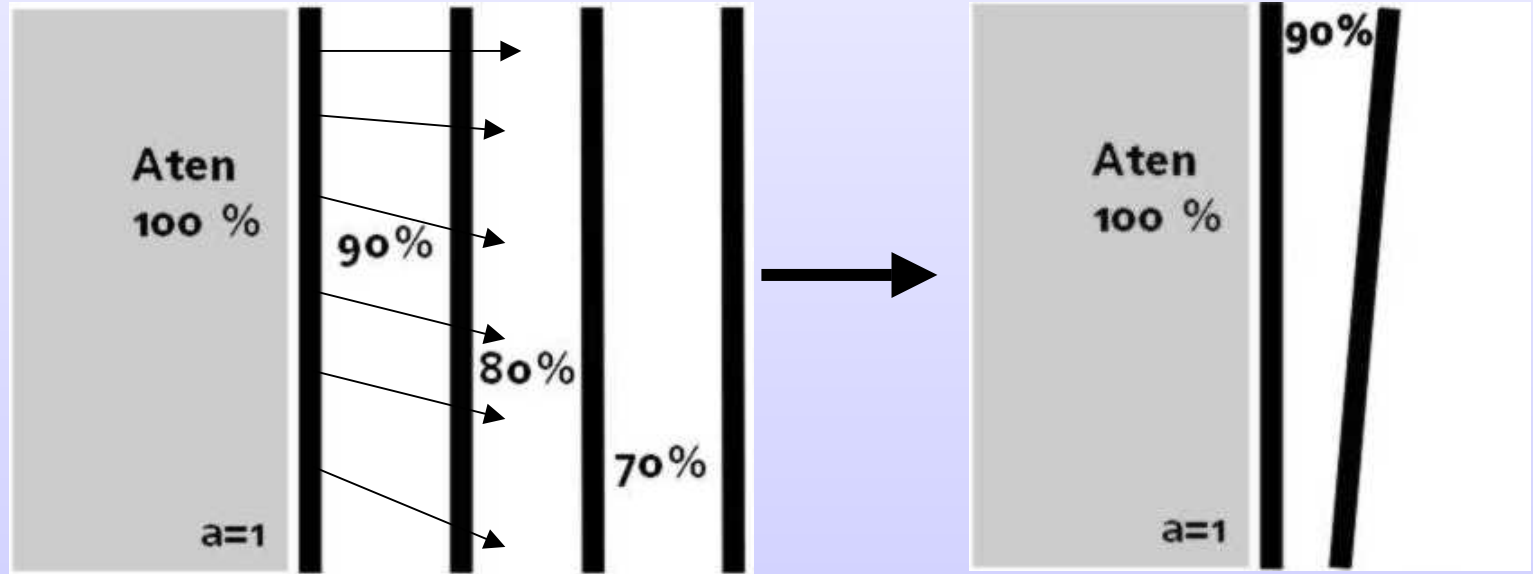




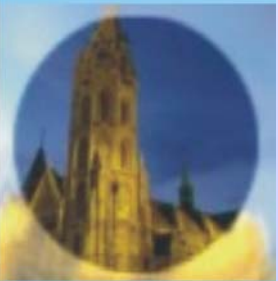
# Fuzzy Classification

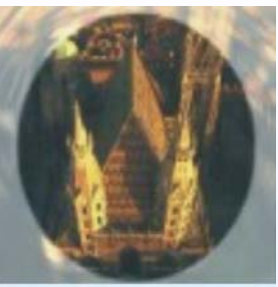
How to construct a membership function for NEAs:

2 ) calculate the direction and the velocity of the motion of an asteroid. This leads to a vector field that can be used to adjust the borders :



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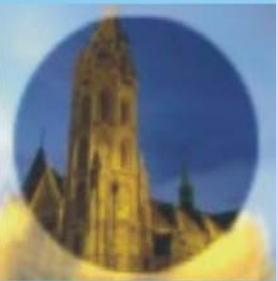


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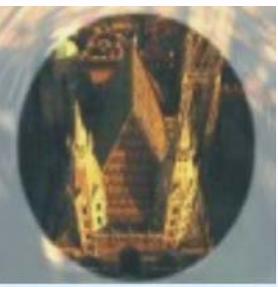
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# Refinement

The fuzzy grouping can be refined by several additional properties of NEAs :

- BCNs
- Collision Probabilities
- Effect of Resonances
- .....



# Conclusions

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- Obtaining a stable grouping of NEAS for long time scales is very difficult
- One needs methods, that are based on the dynamics of the asteroids
- A lot of work is still needing to understand the mixing dynamics of planet crossing asteroids

